

The Vast World of Quantum Advantage

John Preskill
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The vast world of quantum advantage

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Rigor is our touchstone, but quantum advantage will sometimes take us by surprise.

Mind the gap

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Do science for now.

Economic impact will inevitably follow.

Myths around quantum computation before full fault tolerance: What no-go theorems rule out and what they don't

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“It is highly plausible that useful applications may be within reach before full fault tolerance is achieved.”





Edit

Quantum Algorithms: A Call To Action

“We should ... adopt a more exploratory, scrappier approach ... Don’t be too afraid.”

arXiv:2506.19232

Future of Quantum Computing

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Andrew: “There need to be guiding principles.”

Eddie: “Look at physics and see whether there are phenomena you can translate into some algorithmic advantage.”

arXiv:2502.17368

Beyond NISQ: The *Megaquop* Machine

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1M quantum ops or more: Requires QEC, and allows tasks beyond classical, NISQ, or analog quantum.

Realms

Computation

Learning/Sensing

Communication/Crypto

Space

Keystones

Predictability (rigorous evidence)

Typicality (average case)

Robustness (against imperfections)

Verifiability (can check the output)

Usefulness (someone wants the answer)

Ideal quantum advantage: Has all 5 at once.

Predictability / Typicality / Usefulness

Cooling quantum systems to a local energy minimum:

Worst-case hard if $BQP \neq BPP$. Solved by quantum thermal gradient descent.

Random circuit sampling:

Average-case hard if PH does not collapse (and other plausible conjectures).

Quantum phase estimation:

Can lower the energy estimate if input has large energy variance.

Discrete logarithm problem:

Average case is as hard as the worst case.

Decoded Quantum Interferometry applied to Optimal Polynomial Intersection:

Approximation ratio achieved by DQI is rigorously established.

Maybe NISQ is useful after all!

Extended reach of error mitigation as gate error rates improve.

Variational methods: Thread the needle between barren plateaus and classical simulability?

Qualitative insights from quantum dynamics (in 2D).

Will AI eat quantum's lunch?

Training data from quantum
computers, simulators, experiments.

The world of quantum advantage
extends far beyond what we can
rigorously establish.

Reasonable ... but to what extent can
this be formalized as a meta-theorem?

Theorem [Huang 2025, Classical hardness of predicting quantum advantage (informal)]

Decision problem: Does executing a given quantum circuit achieve advantage over classical simulation of that same circuit using low-weight Pauli propagation?

A quantum computer can solve this efficiently; a classical computer cannot unless $BPP = BQP$.

Questions

What quantum heuristics are particularly promising for exhibiting quantum advantage?

What problems exhibit quantum advantage for typical instances drawn from a natural distribution?

What quantum advantages are simultaneously predictable, typical, robust, verifiable, and useful?

What well-motivated complexity conjectures point toward new varieties of quantum advantage?

How should we broaden our toolkit for predicting quantum advantage?

What can we achieve in the next 5 years?